

# A time-efficient video stabilization algorithm based on Block Matching in a restricted search space

Kevin Joseph, Alex Noel Joseph Raj, Zhun Fan, Vidhyapathi CM

**Abstract**— In this paper, we study various video stabilization techniques and develop an algorithm which can perform video stabilization under strict time constraints. To do this, an optimized version of block matching in a restricted search space is utilized to minimize the use of computational resources. We also develop an experimental setup to do real-time video stabilization under various vibrating conditions. In this study, we have also compared our algorithm with an existing stabilization algorithm and looked at how the two techniques perform under different circumstances.

## I. INTRODUCTION

The prevalence of video capturing devices in the modern age is ever increasing and what all these devices have in common is a preview display. This display mirrors the scene that is being captured and it gives the videographer an idea of what the final captured video would be like. In a lot of cases, the video-camera is not mounted on a stationary platform; this results in a jittery video and the preview is also shaky. Our goal is to develop a stabilization algorithm that is fast enough to process the frames as they are captured and to display the preview to the videographer with minimal delay. This gives the videographer a better sense of the scene that is being captured.

We also have self-driving cars, unmanned aerial vehicles, autonomous underwater vehicles, planetary rovers and newly emerging domestic robots which have some sort of video input. The video acquired by these agents are extremely jittery as the cameras are moving about in an unconstrained manner; this reduces the quality of the video. It is essential that the quality of the video be of a certain standard so that the higher level vision systems can process this video information to help in the navigation of these artificial agents. Thus it is important that the raw video feed is stabilized in real time and with minimal delay before being used by the higher level of vision algorithms. The time constraints dictated by these applications are extremely demanding, which is why the stabilization algorithm must be able to process out frames as quickly as they come in with a minimal delay. The primary objective of this study is to develop a robust video stabilization algorithm which would be able to function in real-time while still producing satisfactory stabilization results. Stabilization systems dealing with global motion containing translation, rotation and scaling effects are referred as 3D stabilization. In real-time systems, most proposed stabilization methods only deal with translational

jitter for computing simplicity, and these models are referred as 2D stabilization. In this study, we only deal with 2D digital image stabilization. Video stabilization can also be dealt with in two ways namely post-processing and real-time processing. In post-processing, the video has already been captured and is processed to remove jitter and increase overall quality. This is done in cases where there are no time constraints. However, in real-time processing, the video is corrected in real-time and the stabilized frame is displayed immediately as it is corrected. The crux of these algorithms is that they have to produce reasonable stabilization while still being fast enough such that there is no significant drop in video frame-rate. In this paper we go on to discuss other related works pertaining to video stabilization, a brief overview of 2D video stabilization is also dealt with in the following section. We then present our algorithm and the different stages involved in it. Finally, we discuss the performance of our algorithm with respect to another method and also describe our experimental setup for real-time video stabilization.

## II. RELATED WORKS

This study aims to develop a fast video stabilization algorithm that has the ability to work in multiple scenarios. The proposed algorithm is also compared with the standard stabilization technique that is recommended by the MATLAB documentation which is based on the work by Lee et al [1]. The proposed method in this study aims to work in a wider range of scenes; one of the limitations of Lee et al [1] method is that it often fail terribly to handle videos with large moving foreground objects. Another limitation of their method is that it requires enough detected and tracked features. Thus our study is to improve upon these disadvantages while still being able to run in real-time. Traditional 2D video stabilization methods [2, 3] proceed in three steps: First, a 2D motion model, such as an affine transformation or a projective transformation, is estimated between successive frames using feature point matching or block matching. Second, the parameters of this motion model are temporally low-pass filtered. Third, frame positions are corrected to remove high-frequency camera shaking. While 2D stabilization is useful for general camera de-shaking, it cannot synthesize an idealized 3D camera path because it has no knowledge of the 3D trajectory of the input camera.

In the first step discussed above, namely 2D motion model estimation a common technique used is block matching. The block matching algorithm (BMA) was commonly used for camera motion estimation [4]. However, when there are moving objects in the scene and regions of plain textures the BMA's can often provide erroneous motion

Kevin Joseph and Vidhyapathi CM are from the School of Electronics Engineering at VIT University, India (email: kevinjoseph1995@gmail.com and vidhyapathicm@vit.ac.in respectively).

Alex Noel Joseph Raj and Zhun fan are from the Key Lab of Digital Signal and Image Processing of Guangdong Province at Shantou University, China (email: jalxnoel@stu.edu.cn and zfan@stu.edu.cn respectively)

information in those areas. To overcome this problem, feature matching methods for motion estimation have been applied to video stabilization [3, 5]. The performance of these 2D methods is basically limited in two aspects. One is that a full-frame warp cannot model the parallax induced by a translational shift in viewpoint, and another is that there is no connection between the 2D warp and a 3D camera motion. Therefore, several stabilization algorithms using 3D camera motion have been proposed recently [6–9]. Among them, the content-preserving warping (CPW)-based stabilization algorithm (CPWS) developed by Liu is known as a state-of-the-art method [6]. The CPWS algorithm consists of three stages. First, it recovers the 3D camera motion and a sparse set of 3D, static scene points using an off-the-shelf structure-from-motion (SFM) system. Second, the user interactively specifies the desired camera path or chooses one of three camera path options: linear, parabolic, or a smoothed version of the original; the CPWS algorithm automatically fits a camera path to the input. Finally, a least-squares optimization algorithm that computes a spatially varying warp from each input video frame into an output frame is performed. However, in spite of superior visual performance of the CPWS, the least-squares optimization process at the third stage requires a significant number of calculations. For example, it may take three minutes to warp a single 1280x 720 frame. This delay is unacceptable in cases where the frame processing time has to be around 30ms. Tae [10] presents a fast 3D video stabilization algorithm that provides noticeably less computational cost than the state-of-the-art method with the same stabilization performance. Their proposed algorithm reduced the processing time by up to 14% compared to Liu’s algorithm but is still not fast enough to be implemented for cases where real-time stabilization is required. The proposed technique in this study aims to compensate stabilization performance with the time efficiency. Thus this technique aims to be implemented in situations where the demands of stabilization performance are not as stringent as time-efficiency. Therefore with the time constraint given prime importance, the next section looks into 2D stabilization techniques in more detail.

### III. THE PROPOSED ALGORITHM

Most 2D stabilization techniques follow the below 3 steps (refer to Fig.1) as given in [2] and even our proposed algorithm follows similar steps. In the sections that follow the specifics of the proposed algorithm are discussed.

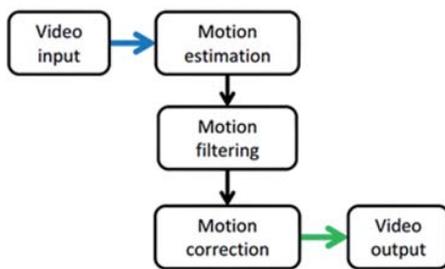


Figure. 1. General 2D video stabilization flow.

#### A. Motion Estimation

For the purpose of stabilization it is required to estimate a motion vector which provides the direction and magnitude by which the current frame in question has moved with respect to the previous frame. A motion vector is estimated at every time instant and is the most computationally expensive stage of any 2D stabilization scheme. The motion vector is often called global motion vector (GMV) and can be found by Full-Search Block method [11]. A block here is defined as a subset of the image. The size of the block is arbitrarily chosen at first. Later, Mean Average Difference (MAD) between the blocks is calculated using equations (1) and (2).

$$MAD(p, q) = \frac{1}{M \times N} \sum_{k=0}^{M-1} \sum_{l=0}^{N-1} \left| I(t-1, x+k, y+l) - I(t, x+k+p, y+l+q) \right| \quad (1)$$

$$\begin{aligned} p &\in \{a+1, a+2, \dots, A-a\} \\ q &\in \{b+1, b+2, \dots, B-b\} \end{aligned} \quad (2)$$

Here ‘I’ is the pixel intensity value at a particular location, ‘M’ and ‘N’ are the sizes of the block, (x, y) is the coordinates of the pixel at the top left corner of the block and t is the frame number. ‘A’ and ‘B’ are the sizes of the frame. The vector (p, q) with the minimum ‘MAD’ is the desired motion vector. The variables ‘p’ and ‘q’ are assigned numbers within the limits of the search area during the search process, in this case being the entire frame. However some values of ‘p’ and ‘q’ will require us to use the pixel-intensity of undefined boundary regions. These regions are avoided. Here, ‘a’ and ‘b’ are the sizes of the boundary of the search space in both axes. Therefore we basically minimize the MAD by searching for the current frame block in the previous frame.

$$GMV = [p \ q] \quad (3)$$

We have the freedom to choose any block size, but if the block size is too small the chances of occurrence of that block in different place is very high, especially in images with repetitive textures and patterns. This will lead to incorrect estimation of the GMV. If the block size is too large, computation time increases but there is also a chance that the scene changed and the block we are trying to locate was not in the previous scene. This again will lead to incorrect motion estimation. For the purpose of real time stabilization, it would be more efficient to choose a small block size. But to ensure that the chosen block does not contain plain surfaces and repeated textures, we perform histogram analysis on multiple small patches and choose the best block out of these. This is discussed below. We select a predetermined number of observation blocks at specific locations in the current frame as illustrated in Fig.2a. Each of these observation blocks is of size  $k \times k$  pixels and the locations of which are known. For our study, we chose  $k=30$  pixels and 3 observation blocks were distributed along the left diagonal of the current frame. We perform a local

histogram analysis on each of the observation blocks to get a statistical distribution of the pixel intensity values. By looking at the variance of the pixel intensity values for the three histograms we select the one highest spread/variance.

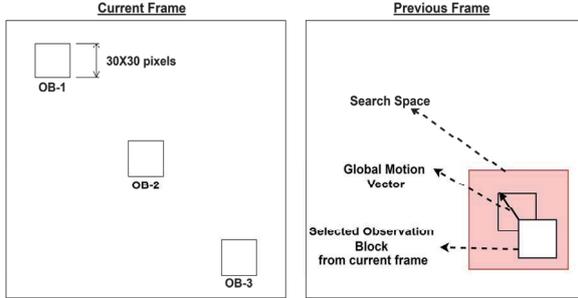


Figure. 2a. Distribution of observation blocks (OB's) in the current frame on the left. Figure. 2b. On the right we have the selected observation block and the search space in the previous block.

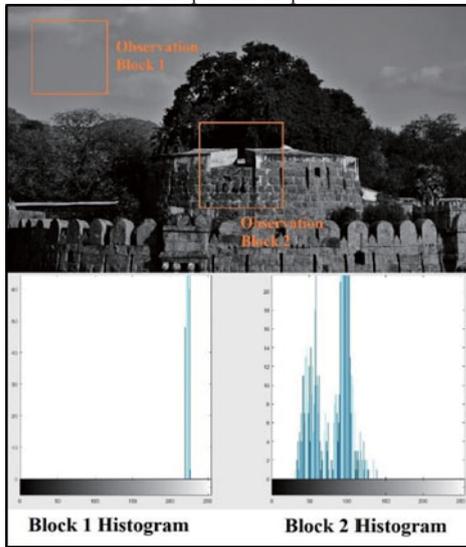


Figure. 3. Two observation blocks in a scene and their corresponding histograms.

Block 2 as shown in the Fig. 3 has more characteristic features and varying pixel values. Block 1, on the other hand, is a plain region. Thus by looking at the histograms, we can arrive at the conclusion that block 2 will be a better candidate to use when trying to estimate the GMV. Once we have selected the observation block from the 3 candidate blocks, we try locating the observation block in the previous frame (refer Fig.2b). It would be a waste of computational resources by keeping the entire of the previous frame as our search space. Thus we limit our search only within a region of interest. It is fairly logical to assume that our region of interest is in the neighborhood of the observation block's original location as it would not have been displaced by a great deal between the two frames. In our study, the region of interest in the previous frame is inclusive of all points the observation block occupied in the current frame and a border surrounding this region which is 5 pixels wide.

After selection of the observation block, we search for the block in the previous frame in a restricted search space as shown in Fig. 2b Mathematically we are performing a similar minimization as shown in (1), the only difference being that

the range of values (p, q) can assume are restricted as given by (4) and (5).

Here 'R' defines the width of the boundary of the search space/region of interest around the location of the observation block. This limited search space allows for fast location of the block in the previous frame. Once we have obtained the values of 'p' and 'q' which minimized the MAD, we assign these values as the elements of the GMV.

$$p \in \{x - R, x - R - 1, \dots, x, x + 1, \dots, x + M - 1 + R\} \quad (5)$$

$$q \in \{y - R, y - R - 1, \dots, y, y + 1, \dots, y + N - 1 + R\} \quad (6)$$

### B. Motion Filtering

The GMV as predicted by the previous section is nothing but a displacement vector which denotes the direction and magnitude of the camera motion in the 2D plane perpendicular to lens's optical axis. This movement can either be intentional camera movement such as panning or unintentional vibration/jitter. It is required of any stabilization system to discern between intentional camera movements and jitter. Once this has been evaluated to compensate for the movement the current frame is moved in the opposite direction of the vibration at that instant. Intentional camera motion is preserved in the process. Jitter/Vibration manifests itself in the trajectory of the camera as the high-frequency component; thus smoothing of the trajectory is nothing but low-pass filtering this signal. One method is called frame position smoothing [12], wherein the GMV is accumulated at every time instant by summing it up. This way the path of the camera is reconstructed in both axes. After the path has been constructed, it can be low pass filtered to smoothen it. However, this low pass filtering has the important drawback of requiring off-line post-processing of sequences. Thus real-time implementation of this technique is not possible. The technique we have used is motion vector integration (MVI) [12] as given by (7).

$$GMV_{integrated}(t) = k \times GMV_{integrated}(t-1) + GMV_{estimated}(t-1) \quad (7)$$

GMV integrated is the motion vector we use to correct the position of the current frame and GMV estimated is the motion vector as predicted by the previous stage of the algorithm. The damping parameter is shown by 'k'. The greater the value of k is, the greater the ability of vibration absorption. In practice, the damping factor was between 0.875 and 0.995 according to the required stabilization intensity [13]. The integrated motion vectors calculated for the present frames are used directly as correction vectors to translate image frames into their stabilized position. Thus the motion vector integration system constitutes a first order IIR filter, that directly low-pass filters the differential motion vectors to remove inter-frame jitter. There are different MVI techniques developed for different scenarios. For example, when the scene which is being stabilized has only jitter and

no intentional camera movements the following technique is used [14].

$$\begin{aligned} GMV_{\text{integrated}}(t) &= k \times GMV_{\text{integrated}}(t-1) \\ &+ (\alpha \times GMV_{\text{estimated}}(t-1)) \\ &+ (1 - \alpha) \times GMV_{\text{estimated}}(t) \end{aligned} \quad (8)$$

In the above equation  $\alpha = 0.75$  and  $k = 0.95$  are used,  $GMV_{\text{integrated}}$  and  $GMV_{\text{estimated}}$  are the same as previously defined. This variant works well in cases where the amplitude of vibration of the camera is high. However, when the camera moves at a constant speed (in an intended direction), a larger  $k$  will make the  $GMV_{\text{integrated}}$  value larger. Due to fixed search range of motion estimation, the ability of vibration absorption will be decreased and the compensated trajectory of  $GMV_{\text{integrated}}$  will lag behind the actual trajectory.

To overcome the issue of constant motion/intentional motion, the vector of constant movement of the camera or constant motion vector (CMV) as given by (10) should be subtracted from the expression as given by (9). This will reduce the size of the correction vector as well as increase the ability of compensation. Therefore, Hsu [15] has added an integrator in the formula to improve this lag problem while the camera is panned at a constant speed. The formula is given in (9):

$$\begin{aligned} GMV_{\text{integrated}}(t) &= k \times GMV_{\text{integrated}}(t-1) \\ &+ (\alpha \times GMV_{\text{estimated}}(t-1)) \\ &+ (1 - \alpha) \times GMV_{\text{estimated}}(t) \\ &- \beta \times CMV(t-1) \end{aligned} \quad (9)$$

$$CMV(t) = CMV(t-1) + GMV_{\text{integrated}}(t) \quad (10)$$

Here the constant  $k$  is used to smooth the playback of camera panning, and constant  $\beta$  is used to filter out abnormal vibrations. However, the compensated trajectory will exceed the original path and oscillate around it in some cases which are referred to as the overshooting phenomena. But these type of aberrations is negligible. These two methods have different advantages and disadvantages. The method proposed in [14] has a better stability in reciprocating motion for motion compensation, but on the other hand, Hsu [15] produced a better performance when there was intentional motion of the camera.

### C. Motion Correction

In our study, we have utilized the method as presented by Hsu. Once  $GMV_{\text{integrated}}$  is calculated at every time instant, we use this as the correction vector to correct the current frame as given by (11). This process happens continuously as new frames are fed from the acquisition device.

$$\begin{aligned} I_{\text{corrected frame}} &= I_{\text{current frame}}(x + GMV_{\text{integrated}}(1), y \\ &+ GMV_{\text{integrated}}(2)). \end{aligned} \quad (11)$$

In cases when the amplitude of vibration is too large the corrected frame will require intensity values at undefined regions of the current regions. The extent of these regions

varies from frame to frame and presents unacceptable visual artifacts. To our knowledge the solution to this problem has not been discussed in the literature, while available software products use frame trimming and magnification or filling by a constant value. These methods lead to severe quality degradation of the resulting video and limit the range of possible correcting transformations (significant transformations lead to large undefined areas). Litvin et al [16] proposed to use mosaicing for each frame in order to exploit temporal correlations between frames. This however is a time consuming process. In this study we have placed a limit on the magnitude on the elements of  $GMV_{\text{integrated}}$  (50 in our case). Thus when correcting the current frame it cannot be displaced by more than 50 pixels along either of the two axes. This ensures that the corrected frame does not have undefined regions.

## IV. RESULTS

### A. Experiment 1: Comparison with stabilization algorithm based on feature trajectories

We used the video sequences which are from <http://pages.cs.wisc.edu/~fliu/project/3dstab.htm> in order to compare our technique with the standard method given by the MathWorks documentation which is based on Lee et al [4]. Their method extracts feature trajectories from the input video. A set of transformations are located by a set of optimizations to smoothen the trajectories and stabilize the video. Their method has the ability to smoothen small rotational variations and translatory vibrations. Their method works exceptionally well except in cases where there is camera rotation and magnification. It produces deformations in the frame as shown in Fig. 5c. Looking at the change in scene between Fig. 5a and Fig. 5b, there is change in scale as well as camera rotation. Their method also fails in cases where there is intentional movement of the camera. The optimization which estimates the geometric transform between every frame is unable to discern the intentional movement when smoothening the trajectory. This is where our technique performs better and at the same time Lee's technique is time consuming as estimating the geometric transform for every frame is computationally expensive.

Another prerequisite for the method presented in [4] is that the video scene must have sufficient number of feature points, in order to estimate the geometric transform. Thus this system will fail in poorly lit scenes and cases where the effect of motion blur is too high. Our method will perform better in these scenarios but still has its limitations. If the scene has a lot of repeated textures and features, the motion estimation stage of our method will predict the wrong motion vector and this will lead to erroneous results [4].

### B. Experiment 2: Real-time stabilization and experimental setup.

For real time implementation we have tested the algorithm on a Windows 7 system running MATLAB 2016 connected to a Logitech C270 web-camera recording at 30

frames per-second. The camera was mounted on a robotic

arm which allowed the camera to move along the horizontal



Figure. 4. The five frames on the top row are from the raw video and the five frames of the bottom row are of the stabilized video.

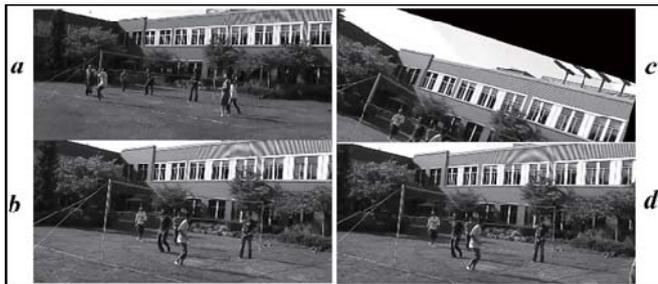


Figure. 5a. The 1st frame in the sequence of the un-stabilized video.

Figure. 5b. The current frame of the un-stabilized video.

Figure. 5c. Depicts the frame as stabilized by Lee's method which is severely distorted.

Figure. 5d. This is the frame stabilized by our method

axis as shown in Fig 6. Vibrations were induced by means of vibration motors attached on the robotic arm and the incoming raw video feed was stabilized in real time. Fig. 4 shows the sequence of frames as captured by the set-up previously described and its stabilized counterpart. We have tracked one particular feature-point in both the sequences and it is seen that the point is displaced less erratically in the stabilized frame. If the right most region of corresponding frames are observed (refer to Fig.4), it is seen that in the raw video the second laptop screen goes out of the frame whereas in the stabilized video the algorithm is able to retain that region in the frame.

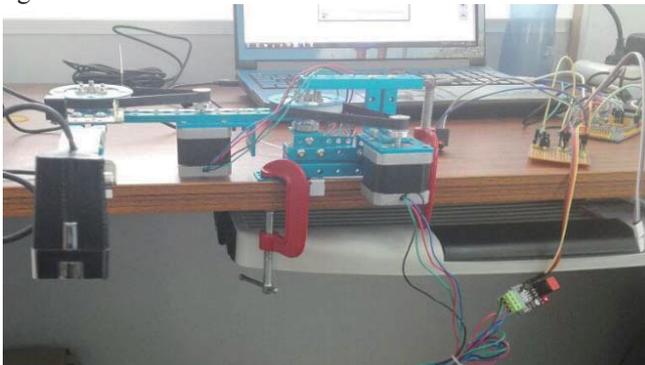


Figure. 6. The experimental setup with the robotic arm on which the video camera was mounted on. The arm could pan along the horizontal axis while vibration motors along the arm would simulate real-life distortions.

This is not that evident in Fig.4 but by tracking the location of that feature in both the axes as each frame passes we get a better estimate of the stabilization performance. The X and Y locations of this feature point is graphically represented in Fig. 7.

The blue lines in Fig.7 denotes the trajectory of a camera panning along the horizontal axis (with and without vibration stabilization). The red line in Fig.7 shows the trajectory along the vertical axis (with and without vibration stabilization). From the graphs in Fig.7 it's worth noting that the *Motion Filtering* stage has retained the intentional camera movements and has simply smoothed out the high amplitude aberrations.

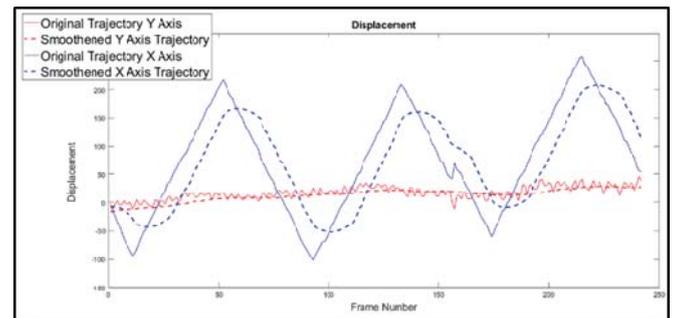


Figure. 7. The red line denotes the path of the feature point in the un-stabilized video whereas the blue line is the stabilized path.

### C. Experiment 3: Effect of damping factor on stabilization performance

In Fig. 8 stabilization algorithm was with different values of the damping factor ( $k$ ). If we look at Fig 8,  $k=0.70$ ,  $k=0.80$ ,  $k=0.90$  and  $k=0.99$  were used in (9) during the stabilization process. With  $k=0.70$ , the stabilized trajectory almost follows the original trajectory of the tracked feature point. But as we progressively go on to increase the value of the 'damping factor' we notice that stabilization performance increases as the path become more stabilized. But if we observe the line corresponding to  $k=0.99$  the smoothing of the path was overdone and a significant part of the original trajectory was distorted and the intentional camera movement was not retained. This manifests itself in the stabilized video as unsynchronized frames and is not visually appealing. Based on experimental observation we chose an optimum value of  $k=0.90$ .

### D. Experiment 4: Effect of block size on stabilization performance

Table I shows how varying the size of the square observation blocks affects performance. In an  $m \times m$  pixel dimension block, we see how performance varies with different values of  $m$ . What can be inferred from the above

table is that as the size of the block is increased the motion estimation system is able to predict motion with increasing accuracy as the mean squared error (MSE) drops (for both the axes) barring some anomalies. It is also observed that as the block size increases the processing time also increases. This is because computing the histogram of larger blocks will progressively take more time. Thus for our real-time implementation, it is essential that a balance between stabilization performance and processing time is found. For our application, we selected a block size of  $m=46$ .

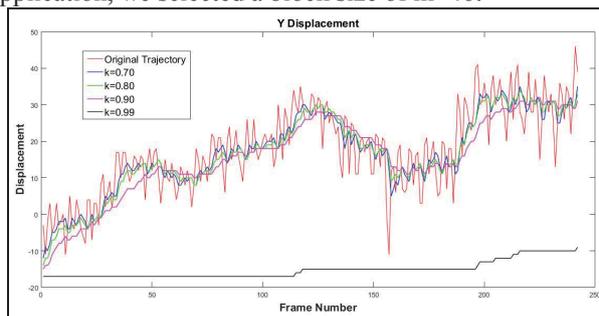


Figure. 8. Here we have the same video sequence stabilized with different values of the damping factor ( $k$ ). We have traced the vertical position of a particular feature point in the above figure (red line).

TABLE I. EFFECT OF BLOCK SIZE

Size of the observation block. ( $m \times m$ pixels)	Mean Squared Error (MSE) between original trajectory and predicted trajectory along X-axis	Mean Squared Error (MSE) between original trajectory and predicted trajectory along Y-axis	Average mean squared error of both axes	Processing time for a 3 second video (s).
20	15.1414	5.0000	10.0707	2.345
26	3.6566	10.5960	7.1263	2.897
30	1.6566	23.3333	12.49495	3.121
36	2.2525	22.7273	12.4899	4.300
40	3.8384	2.8182	3.3283	4.678
46	0.7879	0.7677	0.7778	6.133
50	1.7576	0.6364	1.197	7.643
56	0.1313	0.3232	0.22725	10.311
60	2.9899	4.5354	3.76265	12.614

## V. CONCLUSION

Thus in this paper, we present a robust stabilization technique that has the ability to work in different situations with relatively acceptable stabilization performance. It has been shown how our proposed method performs in comparison with a contemporary standard stabilization technique. Another area of improvement is to equip the algorithm to perform better in cases where there is a change in scale of the scene (magnification) as a result of movement of the camera in the third degree of freedom. The proposed algorithm in its current form is unable to suppress minor rotational movements of the camera. This is another issue that will be addressed in the further study of the topic.

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